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TABLE OF CONTENTS

On direct products of theories. By ANDRZEJ MOSTOWSKI.....	1
An extension of computational logic. By ALAN ROSE.....	32
The system LD. By HASKELL B. CURRY.....	35
On the interpretation of non-finitist proofs—Part II. By G. KREISEL....	43
Reviews.....	59
Über ω -Unvollständigkeit in der Peano-Arithmetik. By G. HASENJAEGGER.	81
On the definition of negation by a fixed proposition in inferential calculus. By HASKELL B. CURRY.....	98
Logic of many-sorted theories. By HAO WANG.....	105
Reviews.....	117
Fourteenth meeting of the Association for Symbolic Logic. By JAMES WILLARD OLIVER.....	156
Abstracts of papers.....	156
Elections.....	159
Problems.....	160
A test for the equality of truth-tables. By JAN KALICKI.....	161
A finitary metalanguage for extended basic logic. By JOHN MYHILL.....	164
Some theorems on definability and decidability. By ALONZO CHURCH and W. V. QUINE.....	179
On reduction to a symmetric relation. By WILLIAM CRAIG and W. V. QUINE.....	188
New notes on simplicity. By NELSON GOODMAN.....	189
A derivation of number theory from ancestral theory. By JOHN MYHILL.	192
Reviews.....	198
Inner models for set theory—Part II. By J. C. SHEPHERDSON.....	225
The axiom of infinity in Quine's New Foundations. By J. BARKLEY ROSSER	238
A note on the theory of quantification. By MOH SHAW-KWEI.....	243
The permutability of rules in the classical inferential calculus. By HASKELL B. CURRY.....	245
The elimination theorem when modality is present. By HASKELL B. CURRY	249
Reviews.....	266
List of officers and members of the Association for Symbolic Logic.....	291

ERRATA

VOLUME 13

Page 164, line 25. Delete the last C in the single axiom for the CN -calculus, and insert C immediately after the first w in the axiom.

VOLUME 14

Page 30, line 6. For the first occurrence of \vee^* , read $^*\vee$.

VOLUME 15

Page 69, line 18. For $2\ 2\ a = a$, read $2\ 2\ a = 2$.

VOLUME 16

Page 5. Interchange lines 30 and 33.

Page 5, line 35. Before « 2.17 », insert « dual of ».

Page 147, line 15 from the bottom. The parentheses should be bold.

Page 224, lines 1 and 4. For *stoiciens*, read *stoiciens*.

Page 270, line 6 from the bottom. For x_2 , read x_2^i .

Page 271, line 12 from the bottom. Before « articulate », insert « be ».

Page 283, line 18 from the bottom. For « Espasa-Calpe », read « Espasa-Calpe ».

VOLUME 17

Page 1. In the last two lines, for « proposition », read « proposition ».

Page 4. At the end of line 5 from the bottom, replace the period by a comma.

Page 5, line 24. Delete the word « inductive ».

Page 9, line 29. For the superior i , read superior i_p .

Page 14, line 4 from the bottom. Add an asterisk at the end of the formula.

Page 15, lines 4 and 6. For I , read I .

Page 17. In line 6, insert a bold dot after $[F_1(x_k)]$; in line 7, for inferior p_μ , read inferior p_ν ; in line 11, for inferior S , read inferior S .

Page 18, line 5. For « is void », read « is void ».

Page 19, line 3 from the bottom. Above the first \mathbf{II} , for P , read p .

Page 20, lines 3–4. Enclose in parentheses the portion of the formula beginning after $(\exists x_p)_1^{m+1}$ and ending before the final bracket; and insert a bold dot after $I_1(x_p)$.

Page 21, lines 1, 3, 10, 11, 15. For P , read P .

Page 22, line 15 from the bottom. For F , read F .

Page 24. In (5), for P , read P ; above the second \mathbf{II} in line 6 from the bottom, for k , read l .

Page 57, line 12. For $\sum_{m=1}^n$, read $\sum_{m=1}^{\infty}$.

Page 57, line 15. For « have », read « has ».

Page 61, line 35. In the signature of the review, read « CHISHOLM ».

Page 66, line 20. Delete the comma before the dash.

Page 76, line 21. For « Principle », read « Principal ».

Page 77, line 8. For « D. B. McCALLUM », read « D. M. McCALLUM ».

Page 77, line 9. For « Electronics », read « Electronic ».

Page 120, line 20. At the beginning of the line, for « einen », read « ein ».

Page 121, line 14. For « gesonderen », read « besonderen ».

Page 131, line 9. The first word in the line should be: « Conceiving ».

Page 150, line 37. For « idoms », read « idioms ».

Page 160, problem 2, line 3. For « functions », read « functionals ».

Page 204. In lines 9 and 18, delete the bold dots which appear after the sign \supset .