



# THE ANZIAM JOURNAL

*(The Australian & New Zealand  
Industrial and Applied  
Mathematics Journal)*

## Editor of The ANZIAM Journal

C. E. M. PEARCE, Department of Applied Mathematics, The University of Adelaide, Australia, 5005;  
cpearce@maths.adelaide.edu.au .

### Associate Editors

A. P. BASSOM  
The University of Exeter  
North Park Road  
Exeter, Devon EX4QE  
United Kingdom  
AP.Bassom@ex.ac.uk

A. J. BRACKEN  
Department of Mathematics  
The University of Queensland  
St. Lucia QLD 4072  
ajb@maths.uq.edu.au

B. D. CRAVEN  
Department of Mathematics  
The University of Melbourne  
VIC 3010  
craven@ms.unimelb.edu.au

A. C. EBERHARD  
Department of Mathematics  
Royal Melbourne Institute of  
Technology  
GPO Box 2476V  
Melbourne VIC 3001  
andrew.eberhard@ems.rmit.edu.au

L. K. FORBES  
School of Mathematics  
and Physics  
The University of Tasmania  
Hobart TAS 7001  
Larry.Forbes@utas.edu.au

J. M. HILL  
Department of Mathematics  
The University of Wollongong  
PO Box 1144  
Wollongong NSW 2500  
j.hill@uow.edu.au

G. C. HOCKING  
Department of Mathematics  
and Statistics  
Murdoch University  
Murdoch WA 6150  
hocking@maths.uwa.edu.au

C. A. HURST  
Department of Physics and  
Mathematical Physics  
The University of Adelaide  
Australia 5005  
ahurst@physics.adelaide.edu.au

P. E. KLOEDEN  
Fachbereich Mathematik  
Johann Wolfgang Goethe  
Universität  
D-60054 Frankfurt am Main  
Germany  
kloeden@math.uni-frankfurt.de

R. MCKIBBIN  
Institute of Information  
and Mathematical Sciences  
Massey University,  
Albany Campus  
Private Bag 102 904  
North Shore Mail Centre  
Auckland  
New Zealand  
R.McKibbin@massey.ac.nz

W. MCLEAN  
Department of Applied  
Mathematics  
University of New South Wales  
Sydney NSW 2052  
W.Mclean@unsw.edu.au

P. K. POLLETT  
Department of Mathematics  
The University of Queensland  
QLD 4072  
pkp@maths.uq.edu.au

D. RALPH  
The Judge Institute of  
Management Studies  
Cambridge University  
Trumpington St  
Cambridge CB2 1AG  
England  
dr241@cam.ac.uk

H. M. SRIVASTAVA  
Department of Mathematics  
and Statistics  
University of Victoria  
Victoria B.C. V8W 3P4  
Canada  
hmsri@uvvm.uvic.ca

K. L. TEO  
Department of Applied  
Mathematics  
Hong Kong Polytechnic  
University  
Hung Hom, Kowloon  
Hong Kong  
mateokl@polyu.edu.hk

A. TORDESILLAS  
Department of Mathematics  
The University of Melbourne  
VIC 3010  
A.Tordesillas@ms.unimelb.edu.au

J.-M. VANDEN-BROECK  
School of Mathematics  
The University of East Anglia  
Norwich NR4 7TJ  
England  
J.Vanden-Broeck@uea.ac.uk

G. C. WAKE  
Department of Mathematics  
and Statistics  
The University of Canterbury  
Private Bag 4800  
Christchurch  
New Zealand  
g.wake@math.canterbury.ac.nz

G. J. WEIR  
Applied Mathematics Centre  
Industrial Research Ltd  
PO Box 31310  
Lower Hutt  
New Zealand  
g.weir@irl.cri.nz

### Executive Editor

E. HUNT, Department of Applied Mathematics, The University of Adelaide, Australia, 5005;  
ehunt@maths.adelaide.edu.au .

### Assistant Editors

Y. STOKES  
Department of Applied Mathematics  
The University of Adelaide, Australia, 5005.

A. GILL  
Land Operations Division, DSTO  
PO Box 1500, Salisbury, SA 5108.

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