

THE  
BULLETIN  
OF  
SYMBOLIC LOGIC

EDITED BY

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VOLUME 8 · NUMBER 1 · MARCH 2002  
ISSN 1079-8986

PUBLISHED QUARTERLY BY THE ASSOCIATION FOR SYMBOLIC LOGIC, INC.  
WITH SUPPORT FROM INSTITUTIONAL MEMBERS

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THE BULLETIN OF SYMBOLIC LOGIC (ISSN 1079-8986) is published quarterly, in the months of March, June, September, and December, by the Association for Symbolic Logic, Inc., 124 Raymond Avenue, Poughkeepsie, NY 12604-0001, USA. Periodicals postage is paid at Poughkeepsie NY and at additional mailing offices. The BULLETIN is distributed with THE JOURNAL OF SYMBOLIC LOGIC; the 2002 annual subscription price for the two journals is \$425. **Postmaster:** Send address changes to *The Bulletin of Symbolic Logic, Journals Division UIP, 1325 South Oak Street, Champaign, IL 61820-6903, USA*. Business correspondence should be sent to the Secretary-Treasurer of the Association, Charles Steinhorn (address on inside back cover).

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*Articles* should be expository or survey papers of broad interest that are accessible to a wide audience of logicians. They may deal with any areas of logic including mathematical or philosophical logic, logic in computer science or linguistics, the history or philosophy of logic, and applications of logic to other fields.

*Communications* should be announcements of important new results and ideas in any aspect of logic: they may be short papers in their final form or preliminary announcements (extended abstracts, position papers) of longer, full papers that will be published elsewhere. In any case, they should include, in addition to a description of the new results or ideas, enough history, background, and explanation to make the significance of the work apparent to a wide audience. *Communications* will be quickly refereed and published within six months of the submission of final versions.

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VOLUME 8  
2002

PUBLISHED QUARTERLY BY THE ASSOCIATION FOR SYMBOLIC LOGIC, INC.  
WITH SUPPORT FROM INSTITUTIONAL AND CORPORATE MEMBERS

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The four numbers of Volume 8 were issued at the following dates:

Number 1, pages 1–184, March 5, 2002

Number 2, pages 185–328, May 25, 2002

Number 3, pages 329–456, August 30, 2002

Number 4, pages 457–634, January 21, 2003

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