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Monte-Carlo techniques for radiotherapy applications I: introduction and overview of the different Monte-Carlo codes

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Abstract

Introduction: The dose calculation plays a crucial role in many aspects of contemporary clinical radiotherapy treatment planning process. It therefore goes without saying that the accuracy of the dose calculation is of very high importance. The gold standard for absorbed dose calculation is the Monte-Carlo algorithm.

Methods: This first of two papers gives an overview of the main openly available and supported codes that have been widely used for radiotherapy simulations.

Results: The paper aims to provide an overview of Monte-Carlo in the field of radiotherapy and point the reader in the right direction of work that could help them get started or develop their existing understanding and use of Monte-Carlo algorithms in their practice.

Conclusions: It also serves as a useful companion to a curated collection of papers on Monte-Carlo that have been published in this journal.

Introduction

The Monte-Carlo method is a statistical random sampling technique for solving complex multidimensional integral equations that are difficult to solve analytically. The general method was introduced in 1949 by Metropolis and Ulam.¹ X-ray interactions at energies of interest in radiotherapy and medical imaging typically result in the production of charged particles such as electrons and positrons. The Boltzmann transport equation can be used to describe the motion of the coupled X-ray and charged particle transport through a defined geometry.^{2,3} An exact deterministic solution to this complex multi-dimensional equation is difficult to obtain, providing motivation for the use of the more efficient statistical Monte-Carlo method to solve the problem. One of the early demonstrations of the value of the Monte-Carlo method for modelling X-ray interactions was published in 1957 by Bruce and Johns.⁴ They showed how the Monte-Carlo method could be used to calculate the spectra of scattered X-rays in water for a radiotherapy X-ray beam. A solution to the problem of using Monte-Carlo methods for simulating the transport of electrons was proposed in 1963 by Berger,⁵ introducing the method known as the condensed history technique. Modelling the transport of ionising radiation using Monte-Carlo lends itself to implementation on digital computers, and Berger notes the implementation of his algorithm on an IBM 704 computer in the FORTRAN computing language. Indeed, it is the increased availability and rapid increase in computing power since the early 1990's that has been a driver for the significant increase in the publication and citation of research into the use of Monte-Carlo for radiotherapy applications. Figure 1 shows the results of a Web of Science search (using the terms 'Monte-Carlo' AND 'Radiotherapy' OR 'Radiation Therapy') that reveals a total of 8419 publications which together have accumulated over 148,000 citations.

The main components of a Monte-Carlo ionising radiation transport simulation are the geometry, the physics models and the cross-section data representing the probabilities of the different physics occurring as a function of energy and material. Developing computer code that accurately encapsulates these three components, particularly for complex geometries is a serious undertaking. However, implementing a basic Monte-Carlo algorithm to model X-ray or gamma ray transport in simple geometries should be within the capabilities of most final-year physics, maths or engineering undergraduate students. The interested reader can find examples of simple implementations of the Monte-Carlo method in two interesting educational papers^{6,7}. Fortunately, for those wishing to accurately model the detailed physics of the coupled X-ray and charged particle interactions in the complex geometries found in radiotherapy and medical imaging, a number of freely available codes are available that require relatively little programming experience. Additionally, Monte-Carlo algorithms are also now a common feature in most of the commercial radiotherapy treatment planning systems.⁸ This has made Monte-Carlo simulation accessible to those interested in the application of the technique to their own user-



Figure 1. Publications (grey bar chart) and citations (red line) from 1957 to 2022 (Web of Science search terms: 'monte carlo' AND 'Radiotherapy' OR 'Radiation Therapy').

specific problem without having to go through the time-consuming process of developing code from scratch.

A constant caveat to the use of Monte-Carlo techniques for simulating radiotherapy treatments is the trade-off between statistical accuracy and the calculation time, known as the efficiency of the simulation. In the context of Monte-Carlo simulations, statistical accuracy is achieved by using a large number of random samples or particle 'histories' e.g. the number of electrons or X-rays, for radiation transport problems. As the number of histories is increased, the calculated quantities e.g. absorbed dose or fluence converge to those expected from real-world measurement. As well as the number of histories, other important factors that influence the statistical accuracy include the quality of the random number generator and the complexity of the physics and geometry models used in the simulation. Improvements in efficiency have been made through the use of variance reduction techniques and parallel processing using multiple Central Processing Unit (CPUs), and more recently, implementation on graphical processing units (GPUs).⁹⁻¹² Variance reduction techniques are methods used to decrease the statistical variability (the variance) of calculated quantities such as absorbed dose or fluence without increasing the computational time, thus improving the efficiency of the use of computational resources.

In this first of two overview papers, we will begin by introducing the reader to the different Monte-Carlo codes that have been most widely used for modelling the different aspects of radiotherapy treatments. A companion paper will provide an overview of the main areas of application in radiotherapy, including modelling the production of beams of ionising radiation for radiotherapy and medical imaging, treatment verification, patient dosimetry and radiobiology.

Monte-Carlo codes

There are a number of Monte-Carlo codes that can be used to model the radiation transport problem. Short introductions to the codes that are freely available, still supported and most widely used in radiotherapy will now follow. It is acknowledged that there are other codes, such as VMC/VMC++ $^{12-17}$ and DPM/gDPM, 12,17

that have been developed and described in the literature over the years but are no longer freely available or supported as stand-alone codes. In some cases, they have been integrated into other more user-friendly or commercial treatment planning systems. The FLUKA code should also be acknowledged, as it is used extensively at CERN for modelling high energy particle physics and has also been used for simulating charged particle and heavy ion radiotherapy.¹⁸

EGSnrc/BEAMnrc/DOSXYZnrc

EGSnrc is one of the most widely used Monte-Carlo codes for radiotherapy and medical imaging applications. It is based on the Electron Gamma Shower (EGS) code developed at the Stanford Linear Accelerator (SLAC),¹⁹ and now maintained by the National Research Council of Canada, and distributed for free (https://github.com/nrc-cnrc/EGSnrc). The code runs on Linux, macOS and Windows operating systems and is able to model the transport of electrons, positrons and gammas with kinetic energies in the range 1 keV to 10 GeV. The code uses an implementation of the condensed history technique for charged particle propagation.²⁰ The code includes user codes with user-friendly graphical user interfaces that simplify the process of modelling the treatment heads of medical linear accelerators and performing patient dose calculations. BEAMnrc comprises component modules that facilitate the modelling of the geometry of components (e.g. target, primary collimator, flattening filter, jaws, MLC, etc.) found in the linear accelerator treatment head.²¹ DOSXYZnrc enables the calculation of dose deposited in voxelised rectilinear geometries including patient models derived from CT data.²² The EGSnrc toolkit maintains flexibility through the inclusion of a wide range of C++ classes, known as egspp, that facilitate the modelling of more complex geometries,.²³

GEANT4

The GEANT4 toolkit was developed at CERN for modelling the passage of particles through matter^{24–26} (https://geant4.web.cern. ch/). Despite its original purpose being the simulation of high

energy physics experiments and detectors, it has been extensively used for radiotherapy applications that include X-ray and particle beam therapy, micro and nano-dosimetry and radiation protection.²⁷ Electromagnetic physics is extended down to energies below 1 keV and up to the TeV range.²⁸ The code is a C++ toolkit that makes use of contemporary object-oriented software engineering principles including the implementation of multi-threading on multi-core computer architectures. The power and flexibility that this design and implementation methodology gives GEANT4 come at the expense of the user being required to have significant prior knowledge and skills of developing applications using a modern C++ toolkit. This has limited its use in the radiotherapy community and has motivated the development of a number of more user friendly software tools that act as an interface or wrapper that makes GEANT4 more accessible to those without object-oriented programming expertise. These include GAMOS,^{29,30} GATE,³¹ PTSIM^{32,33} and TOPAS.^{34,35} A further advantage of the GEANT4 code is the GEANT4-DNA extension (http://geant4dna.in2p3.fr/index.html) that enables modelling of the step-bystep discrete interactions of ionising particles in water at the cellular length scale.³⁶⁻³⁸ Physical, chemical and biological effects of ionising radiation interactions in water can be modelled^{39,40} using GEANT4-DNA.

GATE

The GEANT4 Application for Tomographic Emission (GATE) (http://www.opengatecollaboration.org/) is based on the GEANT4 toolkit and currently enables the simulation of Emission Tomography (PET and SPECT), computed tomography (CT), Bioluminescence and Fluorescence Imaging and Radiotherapy geometries.^{31,41-44} GATE was originally developed for the nuclear medicine community with a primary aim of enabling the end user to model nuclear medicine systems without any requirement for prior knowledge of C++. Instead users use a more intuitive scripting language for creating geometries and setting simulation parameters that can then be run interactively or in batch mode. A feature of GATE is its capability for simulating dynamic or time-dependent aspects of an imaging experiment, for example, a decaying source, source and/or detector movement or breathing motion of a patient.⁴⁵ In more recent times, GATE has been extended to include bioluminescence and optimal imaging^{44,46} and radiotherapy, including particle therapy.^{31,43,47,48}

TOPAS

The TOPAS (Tool for PArticle Simulation) Monte-Carlo code was also developed to make it easier for the medical physicist to perform simulations of radiation transport using the GEANT4 code^{34,35} (www.topasmc.org). Little or no knowledge of the GEANT4 code or the C++ programming language is required by the user. TOPAS simulations are controlled through a userfriendly TOPAS Parameter Control System that wraps the GEANT4 code while maintaining the full functionality of the underlying code including 4D time-dependent simulations. For more advanced users with C++ experience, there is the opportunity to develop their own extensions for integration into the TOPAS code. TOPAS was originally developed to facilitate the simulation of proton and carbon-ion therapy systems and has been used to develop models of passive and pencil beam scanning systems.^{49–51} Despite its particle therapy roots, it is also able to model the more widely used photon and electron beams to the extent that an MV linac example is now included as part of the more recent

releases. Examples of uses for modelling Brachytherapy sources are also provided. TOPAS has also been extended to include the Geant4-DNA radiobiology capabilities,^{52–55} through TOPAS-nBio (github.com/topas-nbio/TOPAS-nBio).

PENELOPE

PENELOPE is able to simulate electron and photon transport⁵⁶ utilising a mixed technique for modelling electron and positron collisions. The latest version, PENELOPE2018, is distributed by the OECD-NEA (https://www.oecd-nea.org/tools/abstract/detail/ nea-1525/). The tools PENGEOM and penGUIn are available to simplify the definition of geometries and running simulations, respectively. PENELOPE has been successfully used to model medical linear accelerators through the extension PENLINAC⁵⁷ as well as the more specialised Tomotherapy^{58,59} and Leksell Gamma Knife systems.^{60,61}

PRIMO

The PRIMO software (https://www.primoproject.net/primo/) enables the simulation of medical linear accelerators and patient dose calculations⁶² using a user-friendly graphical interface. It is slightly different from other radiotherapy Monte-Carlo software in that it is available for free, but is not open source, instead being distributed as a compiled executable that runs in a 64-bit Windows environment. Parallel processing is supported on systems with multicore processors.⁶³ Beneath the intuitive graphical user interface, radiation transport is performed using the PENELOPE and DPM Monte-Carlo codes.^{17,56,64}

The 'dose planning method' (DPM) is a code for simulating the transport of electrons and photons in the context of radiotherapy.¹⁷ The DPM code is designed to offer accurate 3D dose calculations in a fraction of the computational time of some of the other widely used codes. A mixed method for simulating electron and positron interactions is employed, with the choice of charged particle method (interaction-by-interaction or continual energy loss) chosen depending on the magnitude of the energy loss of the charged particle in the interaction. Photon interactions are modelled in an analogue manner.

Earlier versions (still available for download) of the PRIMO software supported both Elekta and Varian accelerator models, but recent versions only contain the Varian models that include a reverse-engineered TrueBeam model known as FakeBeam.⁶⁵ Fakebeam models both flattening filter and flattening filter-free modes.⁶⁶ PRIMO supports the import of DICOM RT Structure and Plan files enabling the simulation and evaluation of clinical IMRT and VMAT treatments.^{67,68} A further study also demonstrated the possibility of calculating patient dosimetry using Varian dynalog files.⁶⁹ Comparisons of PRIMO with other Monte-Carlo codes have shown good agreement.^{70,71}

MCNP

The Monte-Carlo N-Particle (MCNP) code (https://mcnp.lanl. gov/) is a general purpose radiation transport simulation code that is able to track 37 different particle types over a broad range of energies and up to 1 TeV/nucleon.⁷² The MCNP code is available to the worldwide user community, subject to USA national security restrictions and distributed through the Radiation Safety Information Computational Center, part of Oak Ridge National Laboratory. MCNP has been applied to a wide range of medical physics problems⁷³ including the modelling of medical linear accelerators,^{74–78} and imaging systems such as radiotherapy electronic portal imaging devices (EPIDs),^{79–81} CT⁸² and PET/CT.⁸³ MCNP has also been used to develop models for kV intraoperative radiotherapy,^{84,85} Brachytherapy,^{86–88} proton therapy^{89,90} and gamma irradiator devices^{91,92} including the Leksell Gamma Knife^{93,94}

Conclusions

This paper is the first of two to give an overview of the use of Monte-Carlo simulation techniques and their application to radiotherapy. This first part has introduced the different codes that are available and currently supported with the aim of assisting the reader who wishes to develop their own use of Monte-Carlo for clinical or research applications. It is worth noting that many of the commercially available treatment planning systems, including Raystation (RaySearch Laboratories), Eclipse (Varian Medical Systems) and Monaco (Elekta) also now have Monte-Carlo algorithms as part of a suite of algorithms for electron, photon and more recently proton beams.^{11,95-97} Acceptable computational processing times are in some cases achieved through the implementation of these algorithms using GPU technology. The result as we move forward is that the radiotherapy practitioner will increasingly find themselves using Monte-Carlo techniques as part of treatment planning and treatment verification.

References

- Metropolis N, Ulam S. The Monte Carlo method. J Am Stat Assoc 1949; 44 (247): 335–341.
- 2. Duderstadt JJ, Martin WM. Transport Theory. New York: Wiley; 1979.
- do Amaral Rodriguez BD, Vilhena MT. An overview of the boltzmann transport equation solution for neutrons, photons and electrons in cartesian geometry. 2009 International Nuclear Atlantic Conference - INAC 2009. Brazilian Association for Nuclear Energy. 2009.
- Bruce WR, Johns HE. Monte Carlo calculations on the spectrum of scattered radiation produced in water by x-ray beams of interest in radiotherapy. Radiology 1957; 68 (1): 100–101.
- 5. Berger MJ. Monte Carlo calculation of the penetration and diffusion of fast charged particles. Methods Comput Physics 1963; 1: 135–215.
- 6. Arqueros F, Montesinos GD. A simple algorithm for the transport of gamma rays in a medium. Am J Phys 2003; 71 (1): 38.
- Sharifzadeh M, Afarideh H, Khala H, Gholipour R. A Matlab-Based Monte Carlo algorithm for transport of gamma-rays in matter. Monte Carlo Methods Appl 2015; 21 (1): 77–90.
- Chetty IJ, Curran B, Cygler JE et al. Report of the AAPM Task Group No. 105: issues associated with clinical implementation of Monte Carlo-based photon and electron external beam treatment planning. Med Phys 2007; 34 (12): 4818–4853.
- Verhaegen F, Seco J. Monte Carlo Techniques in Radiation Therapy : Introduction, Source Modelling, and Patient Dose Calculations. Boca Raton: Taylor & Francis Group; 2021.
- Seco J, Verhaegen F. Monte Carlo Techniques in Radiation Therapy : Applications to Dosimetry, Imaging, and Preclinical Radiotherapy. Boca Raton: Taylor & Francis Group; 2021.
- Paudel MR, Kim A, Sarfehnia A et al. Experimental evaluation of a GPUbased Monte Carlo dose calculation algorithm in the Monaco treatment planning system. J Appl Clin Med Phys 2016; 17 (6): 230–241.
- Jia X, Gu X, Graves YJ, Folkerts M, Jiang SB. GPU-based fast Monte Carlo simulation for radiotherapy dose calculation. Phys Med Biol 2011; 56 (22): 7017–7031.
- Edimo P, Clermont C, Kwato MG, Vynckier S. Evaluation of a commercial VMC plus Monte Carlo based treatment planning system for electron beams using EGSnrc/BEAMnrc simulations and measurements. Phys Med 2009; 25 (3): 111–121.

- Fippel M. Fast Monte Carlo dose calculation for photon beams based on the VMC electron algorithm. Med Phys 1999; 26 (8): 1466–1475.
- Gardner J, Sievers J, Kawrakow I. Dose calculation validation of VMC++ for photon beams. Med Phys 2007; 34 (5): 1809–1818.
- 16. Ferretti A, Martignano A, Simonato F, Paiusco M. Validation of a commercial TPS based on the VMC (++) Monte Carlo code for electron beams: commissioning and dosimetric comparison with EGSnrc in homogeneous and heterogeneous phantoms. Phys Med 2014; 30 (1): 25–35.
- Sempau J, Wilderman SJ, Bielajew AF. DPM, a fast, accurate Monte Carlo code optimized for photon and electron radiotherapy treatment planning dose calculations. Phys Med Biol 2000; 45 (8): 2263–2291.
- Böhlen TT, Cerutti F, Chin MPW et al. The FLUKA code: developments and challenges for high energy and medical applications. Nucl Data Sheets 2014; 120: 211–214.
- Nelson WR, Hirayama H, Rogers DWO. The EGS4 code system, Report SLAC-265. Standford: Stanford Linear Accelerator Center, 1985.
- Kawrakow I. Accurate condensed history Monte Carlo simulation of electron transport. I. EGSnrc, the new EGS4 version. Med Phys 2000; 27 (3): 485–498.
- Rogers DW, Faddegon BA, Ding GX, Ma CM, We J, Mackie TR. BEAM: a Monte Carlo code to simulate radiotherapy treatment units. Med Phys 1995; 22 (5): 503–524.
- Kawrakow I, Walters BRB. Efficient photon beam dose calculations using DOSXYZnrc with BEAMnrc. Med Phys 2006; 33 (8): 3046–3056.
- Kawrakow I. Egspp: The EGSnrc C++ Class Library. NRCC, 2019. https:// nrc-cnrc.github.io/EGSnrc/doc/pirs898/. Accessed on 10th September 2022.
- Agostinelli S, Allison J, Amako K et al. Geant4—a simulation toolkit. Nucl Instrum Methods Phys Res A 2003; 506 (3): 250–303.
- Allison J, Amako K, Apostolakis J et al. Geant4 developments and applications. IEE Trans Nucl Sci 2006; 53 (1): 270–278.
- Allison J, Amako K, Apostolakis J et al. Recent developments in Geant4. Nucl Instrum Methods Phys Res A 2016; 835: 186–225.
- Arce P, Bolst D, Cutajar D et al. Report on G4-Med, a Geant4 benchmarking system for medical physics applications developed by the Geant4 Medical Simulation Benchmarking Group. Med Phys 2020; 48 (1): 19– 56. doi: 10.1002/mp.14226
- Chauvie S, Guatelli S, Ivanchenko V et al. Geant4 low energy electromagnetic physics. IEEE Symposium Conference Record Nuclear Science 2004; 3: 1881–1885.
- Arce P, Rato P, Canadas M, Lagares JI. GAMOS: A Geant4-based easy and flexible framework for nuclear medicine applications. 2008 IEEE Nuclear Science Symposium Conference Record. 2008. 3162–3168.
- Arce P, Lagares JI, Harkness L et al. GAMOS: An easy and flexible way to use GEANT4. 2011 IEEE Nuclear Science Symposium Conference Record. 2011. 2230–2237.
- 31. Jan S, Benoit D, Becheva E et al. GATE V6: a major enhancement of the GATE simulation platform enabling modelling of CT and radiotherapy. Phys Med Biol 2011; 56 (4): 881–901.
- 32. Aso T, Kimura A, Kameoka S, Murakami K, Sasaki T, Yamashita T. GEANT4 based simulation framework for particle therapy system. 2007 IEEE Nuclear Science Symposium Conference Record, vol 4. 2007. 2564–2567.
- Aso T, Kimura A, Yamashita T, Sasaki T. Optimization of patient geometry based on CT data in GEANT4 for medical application. 2007 IEEE Nuclear Science Symposium Conference Record, vol 4. 2007. 2576–2580.
- Faddegon B, Ramos-Méndez J, Schuemann J et al. The TOPAS tool for particle simulation, a Monte Carlo simulation tool for physics, biology and clinical research. Phys Med 2020; 72: 114–121.
- Perl J, Shin J, Schumann J, Faddegon B, Paganetti H. TOPAS: an innovative proton Monte Carlo platform for research and clinical applications. Med Phys 2012; 39 (11): 6818–6837.
- Incerti S, Baldacchino G, Bernal M et al. The Geant4-DNA project. Int J Modeling, Simulation, Sci Computing 2010; 01 (02): 157–178.
- Bernal MA, Bordage MC, Brown JMC et al. Track structure modeling in liquid water: a review of the Geant4-DNA very low energy extension of the Geant4 Monte Carlo simulation toolkit. Phys Med 2015; 31 (8): 861–874.

- Incerti S, Douglass M, Penfold S, Guatelli S, Bezak E. Review of Geant4-DNA applications for micro and nanoscale simulations. Phys Med 2016; 32 (10): 1187–1200.
- Peukert D, Incerti S, Kempson I et al. Validation and investigation of reactive species yields of Geant4-DNA chemistry models. Med Phys 2019; 46 (2): 983–998.
- Sakata D, Belov O, Bordage MC et al. Fully integrated Monte Carlo simulation for evaluating radiation induced DNA damage and subsequent repair using Geant4-DNA. Sci Rep 2020; 10 (1): 20788.
- Jan S, Santin G, Strul D et al. GATE: a simulation toolkit for PET and SPECT. Phys Med Biol 2004; 49 (19): 4543–4561.
- Sarrut D, Bała M, Bardiès M et al. Advanced Monte Carlo simulations of emission tomography imaging systems with GATE. Phys Med Biol 2021; 66 (10). doi: 10.1088/1361-6560/abf276
- 43. Sarrut D, Bardiès M, Boussion N et al. A review of the use and potential of the GATE Monte Carlo simulation code for radiation therapy and dosimetry applications. Med Phys 2014; 41 (6): 064301.
- Cuplov V, Buvat I, Pain F, Jan S. Extension of the GATE Monte-Carlo simulation package to model bioluminescence and fluorescence imaging. J Biomed Opt 2014; 19 (2): 026004.
- 45. Santin G, Strul D, Lazaro D et al. GATE: a Geant4-based simulation platform for PET and SPECT integrating movement and time management. IEE Trans Nucl Sci 2003; 50 (5): 1516–1521.
- Kang HG, Song SH, Han YB, Kim KM, Hong SJ. Lens implementation on the GATE Monte Carlo toolkit for optical imaging simulation. J Biomed Opt 2018; 23 (2): 1–13.
- 47. Zarifi S, Ahangari HT, Jia SB, Tajik-Mansoury MA. Validation of GATE Monte Carlo code for simulation of proton therapy using National Institute of Standards and Technology library data. J Radiother Pract 2019; 18 (1): 38–45.
- 48. Zarifi S, Ahangari HT, Jia SB, Tajik-Mansoury MA, Najafzadeh M, Firouzjaei MP. Bragg peak characteristics of proton beams within therapeutic energy range and the comparison of stopping power using the GATE Monte Carlo simulation and the NIST data. J Radiother Pract 2020; 19 (2): 173–181.
- Liu H, Zhang L, Chen Z et al. A preliminary Monte Carlo study for the treatment head of a carbon-ion radiotherapy facility using TOPAS. EPJ Web Conf 2017; 153: 04018.
- Lin L, Kang M, Solberg TD, Ainsley CG, McDonough JE. Experimentally validated pencil beam scanning source model in TOPAS. Phys Med Biol 2014; 59 (22): 6859–6873.
- Huang S, Kang M, Souris K et al. Validation and clinical implementation of an accurate Monte Carlo code for pencil beam scanning proton therapy. J Appl Clin Med Phys 2018; 19 (5): 558–572.
- Schuemann J, McNamara AL, Ramos-Méndez J et al. TOPAS-nBio: an Extension to the TOPAS Simulation Toolkit for Cellular and Sub-cellular Radiobiology. Radiat Res 2019; 191 (2): 125–138.
- Ramos-Méndez J, Perl J, Schuemann J, McNamara A, Paganetti H, Faddegon B. Monte Carlo simulation of chemistry following radiolysis with TOPAS-nBio. Phys Med Biol 2018; 63 (10): 105014.
- McNamara AL, Ramos-Méndez J, Perl J et al. Geometrical structures for radiation biology research as implemented in the TOPAS-nBio toolkit. Phys Med Biol 2018; 63 (17): 175018.
- McNamara A, Geng C, Turner R et al. Validation of the radiobiology toolkit TOPAS-nBio in simple DNA geometries. Phys Med 2017; 33: 207–215.
- Baró J, Sempau J, Fernández-Varea JM, Salvat F. PENELOPE: an algorithm for Monte Carlo simulation of the penetration and energy loss of electrons and positrons in matter. Nucl Instrum Methods Phys Res B 1995; 100 (1): 31–46.
- Rodríguez ML. PENLINAC: extending the capabilities of the Monte Carlo code PENELOPE for the simulation of therapeutic beams. Phys Med Biol 2008; 53 (17): 4573–4593.
- Sterpin E, Salvat F, Cravens R, Ruchala K, Olivera GH, Vynckier S. Monte Carlo simulation of helical tomotherapy with PENELOPE. Phys Med Biol 2008; 53 (8): 2161–2180.
- Sterpin E, Chen Y, Chen Q, Lu W, Mackie TR, Vynckier S. Monte Carlobased simulation of dynamic jaws tomotherapy. Med Phys 2011; 38 (9): 5230–5238.

- Moskvin V, DesRosiers C, Papiez L, Timmerman R, Randall M, DesRosiers P. Monte Carlo simulation of the Leksell Gamma Knife: I. Source modelling and calculations in homogeneous media. Phys Med Biol 2002; 47 (12): 1995–2011.
- Moskvin V, Timmerman R, DesRosiers C et al. Monte carlo simulation of the Leksell Gamma Knife: II. Effects of heterogeneous versus homogeneous media for stereotactic radiosurgery. Phys Med Biol 2004; 49 (21): 4879– 4895.
- Rodriguez M, Sempau J, Brualla L. PRIMO: a graphical environment for the Monte Carlo simulation of Varian and Elekta linacs. Strahlenther Onkol 2013; 189 (10): 881–886.
- Rodriguez M, Brualla L. Many-integrated core (MIC) technology for accelerating Monte Carlo simulation of radiation transport: a study based on the code DPM. Comput Phys Commun 2018; 225: 28–35.
- Rodriguez M, Sempau J, Bäumer C, Timmermann B, Brualla L. DPM as a radiation transport engine for PRIMO. Radiat Oncol 2018; 13 (1): 256.
- Rodriguez M, Sempau J, Fogliata A, Cozzi L, Sauerwein W, Brualla L. A geometrical model for the Monte Carlo simulation of the TrueBeam linac. Phys Med Biol 2015; 60 (11): N219–N229.
- 66. Belosi MF, Rodriguez M, Fogliata A et al. Monte Carlo simulation of TrueBeam flattening-filter-free beams using varian phase-space files: comparison with experimental data. Med Phys 2014; 41 (5): 051707.
- Esposito A, Silva S, Oliveira J, Lencart J, Santos J. Primo software as a tool for Monte Carlo simulations of intensity modulated radiotherapy: a feasibility study. Radiat Oncol 2018; 13 (1): 91.
- Paganini L, Reggiori G, Stravato A et al. MLC parameters from static fields to VMAT plans: an evaluation in a RT-dedicated MC environment (PRIMO). Radiat Oncol 2019; 14 (1): 216.
- Rodriguez M, Brualla L. Treatment verification using Varian's dynalog files in the Monte Carlo system PRIMO. Radiat Oncol 2019; 14 (1): 67.
- Aamri H, Fielding A, Aamry A et al. Comparison between PRIMO and EGSnrc Monte Carlo models of the Varian True Beam linear accelerator. Radiat Phys Chem 2020; 178: 109013.
- Lloyd SAM, Gagne IM, Bazalova-Carter M, Zavgorodni S. Validation of Varian TrueBeam electron phase-spaces for Monte Carlo simulation of MLC-shaped fields. Med Phys 2016; 43 (6): 2894–2903.
- Kulesza J, Adams T, Armstrong J et al. MCNP[®] Code Version 6.3.0 Theory & User Manual. Boca Raton: Office of Scientific and Technical Information (OSTI), 2022. doi: 10.2172/1889957
- Solberg TD, DeMarco JJ, Chetty IJ et al. A review of radiation dosimetry applications using the MCNP Monte Carlo code. Radiochim Acta 2001; 89 (4–5): 337–355.
- Mesbahi A, Reilly AJ, Thwaites DI. Development and commissioning of a Monte Carlo photon beam model for Varian Clinac 2100EX linear accelerator. Appl Radiat Isot 2006; 64 (6): 656–662.
- Ezzati AO, Studenski MT, Jamshidi N. A simple source model for 6 MV flattening filter free photon beams Monte Carlo dose calculations. Phys Part Nucl Lett 2021; 18 (7): 791–798.
- Padilla-Cabal F, Pérez-Liva M, Lara E, Alfonso R, Lopez-Pino N. Monte Carlo calculations of an Elekta Precise SL-25 photon beam model. J Radiother Pract 2015; 14 (3): 1–12.
- Bahreyni Toossi MT, Ghorbani M, Akbari F, Sabet LS, Mehrpouyan M. Monte Carlo simulation of electron modes of a Siemens Primus linac (8, 12 and 14 MeV). J Radiother Pract 2013; 12 (4): 352–359.
- Kim JO, Siebers JV, Keall PJ, Arnfield MR, Mohan R. A Monte Carlo study of radiation transport through multileaf collimators. Med Phys 2001; 28 (12): 2497–2506.
- Juste B, Miro R, Diez S, Campayo JM, Verdu G. Monte Carlo simulation of the iView GT portal imager dosimetry. 7th International Topical Meeting on Industrial Radiation and Radioisotope Measurement Application, vol 68. 2010. 922–925.
- Juste B, Miro R, Diez S, Campayo JM, Verdu G. Dosimetric capabilities of the Iview GT portal imager using MCNP5 monte carlo simulations. 2009 Annual International Conference of the IEEE Engineering in Medicine and Biology Society, vol 2009. Embc: 2009 Annual International Conference of the Ieee Engineering in Medicine and Biology Society, vol 1–20. 2009. 3743–3746.

- 81. Juste B, Miró R, Morera D, Díez S, Campayo J, Verdú G. MCNP5 Monte Carlo simulation of amorphous silicon EPID dosimetry from MLC radiation therapy treatment beams. 2012 Annual International Conference of the IEEE Engineering in Medicine and Biology Society. IEEE Engineering in Medicine and Biology Society Conference Proceedings. 2012. 5786–5789.
- Ding AP, Gu JW, Trofimov AV, Xu XG. Monte Carlo calculation of imaging doses from diagnostic multidetector CT and kilovoltage cone-beam CT as part of prostate cancer treatment plans. Med Phys 2010; 37 (12): 6199–6204.
- Waeleh N, Saripan MI, Musarudin M, Mashohor S, Ahmad Saad FF. Modeling and experimental verification of Biograph TruePoint PET/CT using MCNP5. 2020 IEEE-EMBS Conference on Biomedical Engineering and Sciences (IECBES). ieeexplore.ieee.org. 2021. 319–323.
- 84. Aghdam MRH, Baghani HR, Mahdavi SR, Aghamiri SMR, Akbari ME. Monte Carlo study on effective source to surface distance for electron beams from a mobile dedicated IORT accelerator. J Radiother Pract 2017; 16 (1): 29–37.
- Aghdam SRH, Siavashpour Z, Aghamiri SMR, Mahdavi SR, Nafisi N. Evaluating the radiation contamination dose around a high dose per pulse intraoperative radiotherapy accelerator: a Monte Carlo study. J Radiother Pract 2020; 19 (3): 265–276.
- Furstoss C, Reniers B, Poon E et al. Monte Carlo iodine brachytherapy dosimetry: study for a clinical application. J Phys Conf Ser 2008; 102.
- Solc J. Monte Carlo calculation of dose to water of a (106)Ru COB-type ophthalmic plaque. J Phys Conf Ser 2008; 102.
- Reniers B, Verhaegen F, Vynckier S. The radial dose function of low-energy brachytherapy seeds in different solid phantoms: comparison between calculations with the EGSnrc and MCNP4C Monte Carlo codes and measurements. Phys Med Biol 2004; 49 (8): 1569–1582.

- Jette D, Chen W. Creating a spread-out Bragg peak in proton beams. Phys Med Biol 2011; 56 (11): N131–N138.
- Verburg JM, Shih HA, Seco J. Simulation of prompt gamma-ray emission during proton radiotherapy. Phys Med Biol 2012; 57 (17): 5459–5472.
- Rodrigues RR, Grynberg SE, Ferreira AV et al. Retrieval of GammaCell 220 irradiator isodose curves with MCNP simulations and experimental measurements. Braz J Phys 2010; 40 (1): 120–124.
- Moradi F, Khandaker MU, Abdul Sani SF, Uguru EH, Sulieman A, Bradley DA. Feasibility study of a minibeam collimator design for a 60Co gamma irradiator. Radiat Phys Chem 2021; 178: 109026.
- Trnka J, Novotny J Jr, Kluson J. MCNP-based computational model for the Leksell gamma knife. Med Phys 2007; 34 (1): 63–75.
- Banaee N, Asgari S, Nedaie HA. Comparison of penumbra regions produced by ancient Gamma knife model C and Gamma ART 6000 using Monte Carlo MCNP6 simulation. Appl Radiat Isot 2018; 137: 154–160.
- 95. Ali I, Alsbou N, Ahmad S. Quantitative evaluation of dosimetric uncertainties in electron therapy by measurement and calculation using the electron Monte Carlo dose algorithm in the Eclipse treatment planning system. J Appl Clin Med Phys 2022; 23 (1): e13478.
- Richmond N, Allen V, Wyatt J, Codling R. Evaluation of the RayStation electron Monte Carlo dose calculation algorithm. Med Dosim 2020; 45 (2): 159–167.
- Richmond N, Angerud A, Tamm F, Allen V. Comparison of the RayStation photon Monte Carlo dose calculation algorithm against measured data under homogeneous and heterogeneous irradiation geometries. Phys Med 2021; 82: 87–99.