

# Appendix 1

## Table of fundamental physical constants

[From Particle Data Group; *Phys. Lett.* **B592** (2004) 1–1109; *J. Phys.* **G33** (2006) 1–1232; P.J. Mohr & B.N. Taylor, CODATA Recommended Values of the Fundamental Constants: 2002, *Rev. Mod. Phys.* **77** (2005) 1–107; B.N. Taylor & E.R. Cohen, *J. Res. Nat. Inst. Standards and Technology* **95** (1990) 497–523; R.C. Weast & M.J. Astle (eds.), *Handbook of Chemistry and Physics*, CRC Press, Boca Raton, Florida (1973).]

Speed of light*	$c$	299 792 458 m/s
Planck's constant	$h$	$6.626\,069\,3 \cdot 10^{-34}$ J s $\pm 0.000\,001\,1 \cdot 10^{-34}$ J s
Planck's constant, reduced	$\hbar = \frac{h}{2\pi}$	$1.054\,571\,68 \cdot 10^{-34}$ J s $\pm 0.000\,000\,18 \cdot 10^{-34}$ J s $= 6.582\,119\,15 \cdot 10^{-22}$ MeV s $\pm 0.000\,000\,56 \cdot 10^{-22}$ MeV s
Electron charge <sup>†</sup>	$e$	$1.602\,176\,53 \cdot 10^{-19}$ C $\pm 0.000\,000\,14 \cdot 10^{-19}$ C $= 4.803\,204\,41 \cdot 10^{-10}$ esu $\pm 0.000\,000\,41 \cdot 10^{-10}$ esu
Gravitational constant	$G$	$6.674\,2 \cdot 10^{-11}$ m <sup>3</sup> /(kg s <sup>2</sup> ) $\pm 0.001\,0 \cdot 10^{-11}$ m <sup>3</sup> /(kg s <sup>2</sup> )

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\* The value of the velocity of light forms the basis for the definition of the length unit, the metre. 1 m is now defined to be the distance travelled by light in 1/299 792 458 s. The quoted value for the speed of light is therefore exact and without error.

<sup>†</sup> esu = electrostatic charge unit.

Avogadro number	$N_A$	$6.022\ 141\ 5 \cdot 10^{23} \text{ mol}^{-1}$ $\pm 0.000\ 001\ 0 \cdot 10^{23} \text{ mol}^{-1}$
Boltzmann constant	$k$	$1.380\ 650\ 5 \cdot 10^{-23} \text{ J/K}$ $\pm 0.000\ 002\ 4 \cdot 10^{-23} \text{ J/K}$
Molar gas constant	$R (= kN_A)$	$8.314\ 473 \text{ J/(K mol)}$ $\pm 0.000\ 014 \text{ J/(K mol)}$
Molar volume, ideal gas at STP <sup>‡</sup>	$V_{\text{mol}}$	$22.413\ 996 \cdot 10^{-3} \text{ m}^3/\text{mol}$ $\pm 0.000\ 039 \cdot 10^{-3} \text{ m}^3/\text{mol}$
Permittivity of free space <sup>§</sup>	$\varepsilon_0 = 1/\mu_0 c^2$	$8.854\ 187\ 817 \dots \cdot 10^{-12} \text{ F/m}$
Permeability of free space	$\mu_0$	$4\pi \cdot 10^{-7} \text{ N/A}^2$ $= 12.566\ 370\ 614 \dots \cdot 10^{-7} \text{ N/A}^2$
Stefan–Boltzmann constant	$\sigma = \frac{\pi^2 k^4}{60 \hbar^3 c^2}$	$5.670\ 400 \cdot 10^{-8} \text{ W/(m}^2 \text{ K}^4)$ $\pm 0.000\ 040 \cdot 10^{-8} \text{ W/(m}^2 \text{ K}^4)$
Electron mass	$m_e$	$0.510\ 998\ 918 \text{ MeV}/c^2$ $\pm 0.000\ 000\ 044 \text{ MeV}/c^2$ $= 9.109\ 382\ 6 \cdot 10^{-31} \text{ kg}$ $\pm 0.000\ 001\ 6 \cdot 10^{-31} \text{ kg}$
Proton mass	$m_p$	$938.272\ 029 \text{ MeV}/c^2$ $\pm 0.000\ 080 \text{ MeV}/c^2$ $= 1.672\ 621\ 71 \cdot 10^{-27} \text{ kg}$ $\pm 0.000\ 000\ 29 \cdot 10^{-27} \text{ kg}$
Unified atomic mass unit (u)	$(1 \text{ g}/N_A)$	$931.494\ 043 \text{ MeV}/c^2$ $\pm 0.000\ 080 \text{ MeV}/c^2$ $= 1.660\ 538\ 86 \cdot 10^{-27} \text{ kg}$ $\pm 0.000\ 000\ 28 \cdot 10^{-27} \text{ kg}$
Charge-to-mass ratio of the electron	$e/m_e$	$1.758\ 820\ 11 \cdot 10^{11} \text{ C/kg}$ $\pm 0.000\ 000\ 20 \cdot 10^{11} \text{ C/kg}$

<sup>‡</sup> Standard temperature and pressure ( $0^\circ\text{C} \hat{=} 273.15\text{K}$  and  $1\text{atm} = 101\ 325\text{Pa}$ ).

<sup>§</sup> Because of the fact that the velocity of light  $c$  is without error by definition, and because  $\mu_0$  is defined to be  $\mu_0 = 4\pi \cdot 10^{-7} \text{ N/A}^2$ ,  $\varepsilon_0$  is also exact.

Fine-structure constant $\alpha$	$\alpha^{-1} = \left( \frac{e^2}{4\pi\varepsilon_0\hbar c} \right)^{-1}$	137.035 999 11 $\pm 0.000\,000\,46$
Classical electron radius	$r_e = \frac{e^2}{4\pi\varepsilon_0 m_e c^2}$	$2.817\,940\,325 \cdot 10^{-15}$ m $\pm 0.000\,000\,028 \cdot 10^{-15}$ m
Electron Compton wavelength	$\frac{\lambda_e}{2\pi} = \frac{\hbar}{m_e c} = \frac{r_e}{\alpha}$	$3.861\,592\,678 \cdot 10^{-13}$ m $\pm 0.000\,000\,026 \cdot 10^{-13}$ m
Bohr radius	$r_0 = \frac{4\pi\varepsilon_0\hbar^2}{m_e e^2} = \frac{r_e}{\alpha^2}$	$0.529\,177\,210\,8 \cdot 10^{-10}$ m $\pm 0.000\,000\,001\,8 \cdot 10^{-10}$ m
Rydberg energy	$E_{\text{Ry}} = m_e c^2 \alpha^2 / 2$	13.605 692 3 eV $\pm 0.000\,001\,2$ eV
Bohr magneton	$\mu_B = e\hbar/2m_e$	$5.788\,381\,804 \cdot 10^{-11}$ MeV/T $\pm 0.000\,000\,039 \cdot 10^{-11}$ MeV/T
Gravitational acceleration, sea level <sup>  </sup>	$g$	9.806 65 m/s <sup>2</sup>
Mass of Earth	$M_\oplus$	$5.792\,3 \cdot 10^{24}$ kg $\pm 0.000\,9 \cdot 10^{24}$ kg
Solar mass	$M_\odot$	$1.988\,44 \cdot 10^{30}$ kg $\pm 0.000\,30 \cdot 10^{30}$ kg

<sup>¶</sup> At a four-momentum transfer squared  $q^2 = -m_e^2$ . At  $q^2 = -m_W^2$  the value is approximately 1/128, where  $m_W = 80.40$  GeV/c<sup>2</sup> is the mass of the  $W$  boson.

<sup>||</sup> Exact by definition. Actually  $g$  varies for different locations on Earth. At the equator  $g \approx 9.75$  m/s<sup>2</sup>, at the poles  $g \approx 9.85$  m/s<sup>2</sup>.