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W. LEWIS, M.A.
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PROCEEDINGS
OF THE
CAMBRIDGE PHILOSOPHICAL SOCIETY
VOLUME 29

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BY WALTER LEWIS, M.A.

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