

Establishing a practical coding scheme computationally measure concept maps

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ABSTRACT: This paper presents a systematic method and coding scheme to convert concept maps into bi-partite graphs that can be computationally evaluated for topological complexity measurements. The coding scheme is focused on splitting concepts with multiple elements embedded and linking these objectively. The guidance for this is established and the method presented with examples. The motivation for this work is to establish a means to objectively compare concept maps generated by individuals at the beginning and the end of an intervention to measure the impact of the intervention. The reliability of the coding scheme is presented in separate work.

KEYWORDS: design education, complexity, design cognition

1. Need for measurement of concept maps

Concept maps are particularly effective in capturing and assessing learning by representing a learner's knowledge structure (Grundspenkis & Strautmane, 2010; Patel et al., 2024; Tergan et al., 2006). They help educators identify misconceptions (Novak, 2010), evaluate conceptual understanding (Maria Araceli Ruiz-Primo et al., 2001; Watson et al., 2016), and track the evolution of knowledge over time (West et al., 2002). For example, comparing pre- and post-intervention concept maps can reveal how learning progresses and what gaps remain (Kamble & Tembe, 2013; Patel et al., 2024). In engineering and design, concept maps are used for brainstorming (Trochim & Kane, 2005), system understanding (Chang, 2007; Padilla et al., 2017; Reichherzer & Leake, 2006), and design process visualization (Correia et6al., 2008; Crampes et6al., 2006). They allow for the integration of multidisciplinary knowledge and support collaboration by providing a clear and shared understanding of a system or process (Arias et al., 2000). Concept maps also play a critical role in knowledge/project management (Cañas et al., 2005; Gamble, Paul R., 2001), preserving best practices (Control et al., 2008) and facilitating the transfer of information across teams and stakeholders (Le Bras et al., 2018; van Bon-Martens et al., 2014).

In engineering education, they serve as tools for promoting metacognitive reflection, helping students connect theory with practical applications and fostering deeper engagement with the material (Besterfield-Sacre et al., 2004; Darmofal et al., 2002; Schroeder et al., 2018; Van Zele et al., 2004; Watson et al., 2016). By analysing the concept maps, researchers can evaluate the richness and depth of the data (Henry, 1974), information (Gamble, Paul R., 2001) and knowledge integration (Dewey, John, 1949), offering insights into both individual (Tergan et al., 2006) and team learning processes (de Ries et al., 2022; Lopez et al., 2014; Novak, 2010; Torre et al., 2007). However, earlier research has not established clear guidelines to encode computationally and measure the complexity of the maps.

The need also extends the tool to be used as a mixed-methods tool delivering both qualitative and quantitative insights as needed while another research states that concept maps were used only for qualitative analysis (Khajeloo & Siegel, 2022; Kinchin et al., 2010). Thus, allowing one to measure micro trends pertaining to an individual participant and their journey; as well as macro trends pertaining to multiple participants and the larger trends as a cohort (D'Antoni et al., 2009).

2. Establishing the concept map coding scheme

The presented concept map coding scheme was developed as part of a larger study and analysis of participants using concept maps for aligning and measuring the engineering identity of undergraduate engineering students identity (Kumar & Summers, 2024). Here, for consistency of terminology, coding is used for three common terms:

- Coding (Carley, 1993; Jackson & Trochim, 2002; Kinchin et al., 2010)
- Rating (Allen et al., 2015; Cañas et al., 2015; Schau et al., 2001)
- Scoring (D'Antoni et al., 2009; McClure et al., 1999; M Araceli Ruiz-Primo, 2004; Rye & Rubba, 2002; Van Zele et al., 2004; West et al., 2002).

The concept maps are also viewed as a tool to measure, understand, or investigate the mental models to understand the perceptions of its participants. By using concepts or keywords (vertices) and connections between the keywords (edges), the graphs represent the conceptualized information for the modeler. For the scope of this research, concept maps are analysed for three things:

- 1) Topology: In this step, complexity metrics (J. Mathieson & Summers, 2017) are captured during the codification of the concept maps are analysed. This helps us understand the type of concept map expected and what its complexity can be attributed to.
- 2) Vocabulary: This step analyses all the keywords, words and sentences, the trends that emerge from these words, along with sentiment and correlation/semantic (LSA) scores.
- 3) Comprehensive: This step combines the two other steps and analyse the concept maps to observe larger trends that emerge in larger categories and classifications.

Coding of the concept maps into its respective sub formats must be uniform, accurate, and consistent. The coding scheme should mitigate bias of evaluators. The final coded concept map should be in a computationally interpretable form that can extract structural complexity metrics (J. L. Mathieson & Summers, 2010a). Finally, for this paper, only "Topology," is considered as it was observed to be the most complicated item demanding a systematic coding scheme.

2.1. Process

The process of coding concept maps accurately and efficiently without the risk of introducing additional complexity and variables boils down developing this robust training manual and a guidebook.

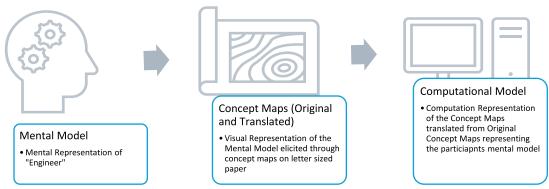


Figure 1. The coding process

The training manual presents a step-by-step procedure to code the concept maps while the guidebook serves as a dictionary with types, scenarios, and examples encountered when coding the vertices and edges of the concept maps. Each concept map is treated like a fingerprint, that is unique to every person (Chang, 2007; Hamdiyati et al., 2018; Moon et al., 2018). Figure 1 illustrates this process and provides a quick snapshot on the entire process of using the original concept maps that capture a central idea in this case, the student's definition of "Engineer" which is then translated to an intermediate step and then to the final computational model.

2.2. Guidebook

The guidebook serves as a preliminary document that details the various issues and complexities while dealing with different individuals and their concept maps. As different individuals use different styles of

expression, thought, opinion, writing, and diagramming, it is important to capture the different scenarios one would encounter while coding concept maps. The guidebook becomes a master key to unlock those variations and develop a consistent understanding of these diverse scenarios. Building objectivity in this work is a central goal. Hence, the guidebook is developed to ensure anyone looking at the concept maps will be able to arrive at the same conclusion and understanding of the participant's mental model. The guidebook presented to the researchers who were coding the concept maps had four sections:

- Summary
- Type V-Vertex (Grundspenkis & Strautmane, 2010; Maria Araceli Ruiz-Primo et al., 2001)
- Type E-Edge (Reichherzer & Leake, 2006)
- Type O-Overall (Lopez et al., 2014; Van Zele et al., 2004; Watson et al., 2016)

Each of these types of complication explored several scenarios within the types and several cases within scenarios accordingly. These categorization of into Type, Scenario and Case allowed the research to create a needed training guidebook and manual aiding the development of a robust coding scheme that can be tested.

2.2.1. Type V-Vertex

The vertices contain the concepts, typically represented as words or phrases and are considered as the data or facts presented by the participant/creator of the concept maps. These vertices must be coded appropriately to retain the essence of the concept map. If there are multiple concepts embedded in a single vertex, it is important to split the vertex to more accurately represent the complexity of the graph. This may increase or decrease the complexity metrics and its values for concept maps, but this guide is to ensure research maintains consistency in the understanding and the coding of the concept maps. This type captured three scenarios

- Independent Terms
- · Only Nodes

still be separated.

· Mathematical

While Only Nodes, and Mathematical has just one case under them, Independent Terms had four cases under it, showcasing the complexity of vertices that can be present in concept maps. These are illustrated through scenarios, cases, and examples in Table 1.

Table 1. Type V-Vertex related scenarios and cases capturing complexity during coding

Scenario	Case	Example
code in the spreadsheet sheet but analysis. Thus, this will have to be	athematical expressions which is hard to can be used in the observations and other e coded as "Product" as a vertex, "greater oney" as another vertex and in this flow	Type V > Mathematical
in the vertices can be separated an represented independently in the spreadsheet format and yet the would not compromise the integrity and accuracy of the concept map and its	s Combo Nodes - "Teamwork + d Leadership" are combined and e connected unidirectionally to y "Engineer" as seen in the screenshot e of the concept map. Split the e Teamwork + Leadership into two s vertices. There could be vertices that e use plus, and, coma, etc. symbols to e have combined elements.	Type V > Independent Terms > Combo Nodes
these keywords are unique and are independent from each other. can be assumed that the participar combined these words to save space or be coherent in the thought process or wanted to cluthem as it made sense to them, but	terminate the Bullet List - Coding this way of the representation increases complexity and the scores due to the introduction of more that vertices and edges but ensures the consistency across maps with similar that cases. Skills will connect to the three that bullet points as bidirectional, but the that bullet points will remain unconnected and coded as unrelated to each other.	Creative team oriented Problem Solver Type V > Independent Terms > Bullet

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List

2.2.2. Type E-edge

The edges are represented as the connections or arcs on the concept maps that represent the flow of information emerging from one of the vertices (data or facts) and ending at another. Similar to 'Type-V,' this complexity type 'Type-E' identified three scenarios to be covered in the coding scheme. Here again the coding scheme emphasizes to categorise and capture the edges to reflect the original intent of the concept map and its creator.

- Overlook analysed edges and their terms, identifying cases within this scenario where certain edges can be simplified or eliminated or reduced also ensuring to stay within an allowable deviation of added or reduced complexity. This scenario captured five cases: i. Use and Discard, ii. Dead Ends, iii. Pit Stop, iv. Slink, and v. Crossover
- Disjoin Terms this scenario identified filler or connection words associated with arcs. While these terms were repeating, they are captured separately to preserve their uniqueness and allow for accurate replication in the coding scheme. Ensuring assumptions are eliminated to second guess the creator of the concept map. Although repetitions are impossible on vertices, it is a common occurrence in edges, as these terms often explain flow of information which can be overlapping. This scenario captured four cases: i. Multiple Repeats, ii. Divergent, iii. Convergent, and iv. Reduction
- Directionality of Flow this scenario examines contradictions and complexities in mapping the directionality of flow. It focuses on understanding the significance of arrow marks, or the ambiguity in determining these connections and their purpose as intended by the creator. This scenario covered four cases: i. Inconsistent, ii. Squiggles, iii. Self-Loop, and iv. I Guess So (IGS)

2.2.3. Type O-overall

'Type O' covers concept maps that do not fit into Type V or Type E or they have multiple types that apply to them. This type applies to checking the maps at the overall level rather than vertices or edges level. Thus, this type often applies to maps that are hybrid with two or more types. Type O includes two scenarios:

- 'Refer The Original' (RTO) concept maps that are hard to read or code initially are flagged before coding for Type V or Type E. The reason behind such maps are a writing utensil that is not appropriate for the task, or the map had illegible handwriting, or a bad scan rendering the digital copy of the concept map, unreadable. Two cases explored: i. Ghosted, and ii. Illegible.
- 'Null Graphs' concept maps were regarded as a null entry, as this map would not have any data to capture or code. Two cases presented were: i. Dummy Map, and ii. Blanks.

2.3. Training manual

The training manual serves as a step-by-step procedure-based manual that helps the coders to code and translate the concept maps into the spreadsheet files. This is done as a three-step process as illustrated in Figure 2.

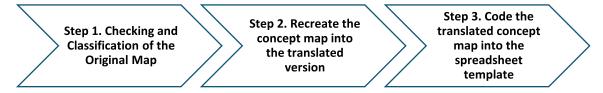


Figure 2. Concept maps three-step coding process

2.3.1. Step 1. Checking and classification of the original concept map

For this step we classify and rate the concept maps on the following attributes: TSC, Readability, Relevance of Information, Completeness, Complexity. This step is to create a quick access meta-data classification and verification called as 'Summary' for the research. Thus, providing a quick and easy classification of the concept map. The real emphasis of coding concept maps is not the summary but, on

the final, spreadsheet file. This is because of the downstream activity after these steps, where the spreadsheet files are used to generate the 27-complexity metrics using MATLAB for every concept map (J. L. Mathieson & Summers, 2010b; J. Mathieson & Summers, 2017). The summary classification and verification is only a check and balancing step in the entire process.

2.3.2. Step 2. Recreate the concept map into the translated version

This is a step focusses on the guidebook and manual to code the vertices and edges, to enable markup on the existing concept map or to redraw the concept map into the translated system of maps which can help convert any concept map into a bi-partite graph that is needed for the analysis. There are six sub-steps which will be detailed with an example below.

2.3.3. Step 3. Code the translated concept map into the spreadsheet template

Each participant will have their own spreadsheet file to maintain the accuracy and consistency from the translated map to the computational map, that is their computational version of the original hand-drawn concept map. Hence creating copies of the file shared and renamed to its corresponding participant ID. Multiple examples are provided to researchers to explain the process, but brevity dictates this paper to present two that illustrate the three-step process. Only the first example will be detailed and while the other example is to help arrive at the required training and conclusion faster.

2.4. Example - NE22NA37:

Figure 3 illustrates a screenshot of the concept map used for this example to detail the coding process.

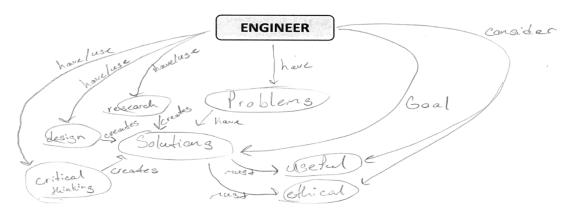


Figure 3. Example 1 – NE22NA37 concept map original

2.4.1. Step 1 - checking and classification

In this step we check the Code, TSC (NA, Single or Multiple), Readability, Relevance of Information, Completeness, and Complexity for the original map and code them in spreadsheet as per *Table 2*. This meta level view of the concept map is used to identify the maps that might need more systematic review by multiple raters.

Table 2. classification of 'Summary' for example 1

Code	TSC	Readability	Relevance of Information	Completeness	Complexity
NE22NA37	Single	High	Medium	Complete	Medium

2.4.2. Step 2: Sub-Step-By-Sub-Step translation of the concept map for this example:

Combining Sub-Steps 1 to 6: Translate Vertices starting from "Engineer" and radiating outward, one level at a time: Radiate outward to the next level or layer. Labelling all the vertices from (A) to (H) in green rectangular and circular boxes, edges are named from [R1] to [Rn] as an interim to finally be named from (I) to (U) in the blue hexagons in figure below to finally be consistent as required for the spreadsheet coding. Once the coding is completed the number of vertices and edges are noted and cross-checked with the record from the summary. Next, all vertices and edges are checked on their assigned alphabets to

match the spreadsheet conversion, thus leaving nothing but the alphabetical representation that is needed to convert any concept map into a bi-partite map (Figure 4). Again, for this coding, only the complexity of the concept map as defined through the graph structural complexity is explored. Other semantic coding that is out of scope may be done separate on the vocabulary that is used in the graph.

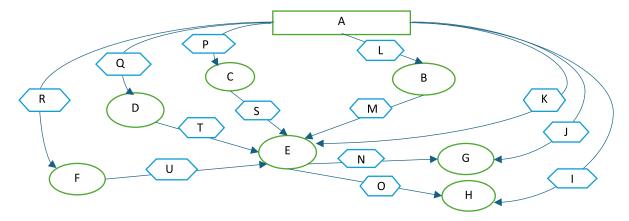


Figure 4. Step 2 final translated map

2.4.3. Step 3 - Concept Map Coded on Spreadsheet and Verification

This step shown in Table 3 highlights that all the unique identifiers assigned to the vertices and the connections/edges. As the concept maps might be directed networks, the edge direction is also captured. The input and output sections are driven by a formula that is connected to the source and sink columns. The researcher coding will meticulously input the source and sink with its newly assigned alphabet in the name column, while everything else mentioned by the participant in the original concept map goes into the description section. The input and output columns can be used to verify the coded concept maps on spreadsheet to the translated and to the original. Everything on the spreadsheet should map back to the original when reverse coded. The translated concept maps and the spreadsheet will be the same and is used during initial training only. This check shows that the original map would have an inherent complexity as observed by the coder and recorded, while the spreadsheet might slightly vary depending on the Type, Scenario and Case that the coder encountered to code the concept maps in spreadsheet that can be used by the research for further analysis.

Table 3. Coding on spreadsheet for example 1

Name	Description	Input	Output	Source	Sink
A	Engineer	0	7	A	I
В	Problems	1	1	I	Н
C	Research	1	1	A	J
D	Design	1	1	J	G
E	Solutions	5	2	A	K
F	Critical Thinking	1	1	K	E
G	Useful	2	0	A	L
H	Ethical	2	0	L	В
I	Consider 1 (R1)	1	1	A	P
J	Consider 2 (R2)	1	1	P	C
K	Goal (R3)	1	1	A	Q
L	Have 1 (R4)	1	1	Q	D
M	Have 2 (R5)	1	1	A	R
N	Must 1 (R6)	1	1	R	F
O	Must 2 (R7)	1	1	В	M
P	Have/Use 1 (R8)	1	1	M	E
Q	Have/Use 2 (R9)	1	1	E	N
R	Have/Use 3 (R10)	1	1	E	O
S	Creates 1 (R11)	1	1	N	G
T	Creates 2 (R12)	1	1	O	Н

(Continued)

Table 3. Continued.

Name	Description	Input	Output	Source	Sink
U	Creates 3 (R12)	1	1	С	S
				D	T
				F	U
				S	E
				T	E
				U	E

2.4.4. Verification

Table 4 shows the final format arrived after the original map from Figure 2, translated to map from Figure 3 and final spreadsheet format from Table 3. In this case since the complexity was with the "EDGES", the coding scheme arrived at all formats having the same vertices and edges. Thus, completing the coding of the concept maps from its original hand-drawn visual form to the spreadsheet form.

Table 4. Verification of vertices and edges from original to spreadsheet format for example 1

Part Type	Original Map	Translated Map	Spreadsheet Format
Vertex (Elements)	8	8	8
Edge (Connections)	13	13	13

2.5. Example 2 - IA10WE93

(Figure 6 shows the original concept map for a second example which is shown in the next page.) Step 1: Summarization of classification as step 1 shown in Table 5.

Table 5. Summary classification for example 2 - IA10WE93

Code	TSC	Readability	Relevance of Information	Completeness	Complexity
IA10WE93	Single	High	Medium	Complete	Medium

Step 2: Figure 5 is a snapshot of the interim translated map just before the final alphabetical translation. Step 3: Snippet of step 3 showing the final verification in Table 6.



Figure 5. Snapshot of hand-drawn translated map as part of step 2

Table 6. Verification of vertices and edges from original, spreadsheet format

Part Type	Original Map	Translated Map	Spreadsheet Format
Vertex (Nodes/Elements)	19	20	20
Edge (Arcs/Connections)	18	20	20

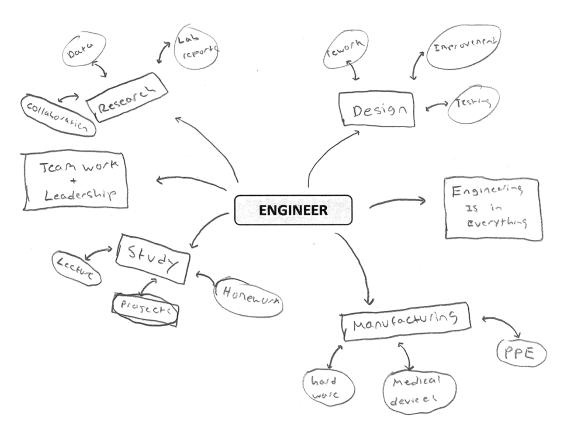


Figure 6. Example 2 - IA10WE93 original concept map

3. Conclusion

This paper establishes a need for a robust coding scheme that can be used to capture the various complexities emerging from hand-drawn or digital concept maps used in mixed methods research, as an augmenting or surrogate tool to provide qualitative and quantitative results. The coding scheme and the process outlined in this article can also be useful to code other flow charts and diagrams which can help store and retrieve information for further processing. The coding scheme established is a simple three step process to capture the data (vertices), information (edges) and knowledge (overall meaning and purpose) from the original concept map which represents the mental model from participants for the topic of interest. The scope of the coding scheme was also established highlighting the limitation with the 'Summary' aspect of concept maps which needs to be further strengthened. The emphasis was on the vertices and edges which form the basis for the structural complexity analysis.

With the coding scheme established, it is being applied to roughly 2,600 concept graphs generated as part of a study on evolution and change within subjects in terms of engineering identity. The concept graphs are expected to increase in complexity from the beginning of the semester to the end of the semester. With the generated graphs, the complexity metrics and be used to measure this change. The larger study is being conducted to collect data through surveys and concept maps to measure the engineering identity of engineering students at an R1 university in the sub-urban region of a metropolitan city in the U.S (Kumar & Summers, 2024). The established coding scheme is intended to be used in this case and will be tested for its accuracy and consistency through the tests for interrater reliability (IRR). The coding scheme is intended to be tested on multiple concept maps with varying complexity (types, scenarios and cases) by multiple rates at different time intervals. This method of testing will help provide a scientific case study-based validation that comes with a high confidence level as demanded by rigorous statistical methods.

References

Allen, M. L., Schaleben-Boateng, D., Davey, C. S., Hang, M., & Pergament, S. (2015). Concept mapping as an approach to facilitate participatory intervention building. *Progress in Community Health Partnerships: Research, Education, and Action*, 9(4), 599–608. https://doi.org/10.1353/cpr.2015.0076

Arias, E., Eden, H., Fischer, G., Gorman, A., & Scharff, E. (2000). Transcending the Individual Human Mind—Creating Shared Understanding through Collaborative Design. *ACM Transactions on Computer-Human Interaction*, 7(1), 84–113. https://doi.org/10.1145/344949.345015

- Besterfield-Sacre, M. E., Gerchak, J., Lyons, M., Shuman, L. J., & Wolfe, H. (2004). Scoring Concept Maps: An Integrated. *Journal of Engineering Education*, April, 105–115.
- Cañas, A. J., Carff, R., Hill, G., Carvalho, M., Arguedas, M., Eskridge, T. C., Lott, J., & Carvajal, R. (2005). Concept maps: Integrating knowledge and information visualization. *In Lecture Notes in Computer Science (including subseries Lecture Notes in Artificial Intelligence and Lecture Notes in Bioinformatics): Vol. 3426 LNCS*. https://doi.org/10.1007/11510154_11
- Cañas, A. J., Novak, J. D., & Reiska, P. (2015). How good is my concept map? *Am I a good Cmapper? Knowledge Management and E-Learning*, 7(1), 6–19. https://doi.org/10.34105/j.kmel.2015.07.002
- Carley, K. (1993). Coding Choices for Textual Analysis: A Comparison of Content Analysis and Map Analysis. *Sociological Methodology*, 23, 75. https://doi.org/10.2307/271007
- Chang, S. N. (2007). Externalising students' mental models through concept maps. *Journal of Biological Education*, 41(3), 107–112. https://doi.org/10.1080/00219266.2007.9656078
- Control, P. P., Performance, P. M., & Contexts, D. (2008). Project Portfolio Control and Portfolio. *Project Management Journal*, 39(4), 28–42. https://doi.org/10.1002/pmj
- Correia, P. R., Infante-Malachias, M. E., & Godoy, C. E. (2008). From theory to practice: the foundations for training students to make collaborative concept maps. *Proceedings of the Third International Conference on Concept Mapping*, 414–421.
- Crampes, M., Ranwez, S., Villerd, J., Velickovski, F., Mooney, C., Emery, A., & Mille, N. (2006). Concept maps for designing adaptive knowledge maps. *Information Visualization*, 5(3), 211–224. https://doi.org/10.1057/palgrave.ivs.9500127
- D'Antoni, A. V., Zipp, G. P., & Olson, V. G. (2009). Interrater reliability of the mind map assessment rubric in a cohort of medical students. *BMC Medical Education*, 9(1), 1–8. https://doi.org/10.1186/1472-6920-9-19
- Darmofal, D. L., Soderholm, D. H., & Brodeur, D. R. (2002). Using concept maps and concept questions to enhance conceptual understanding. *Proceedings Frontiers in Education Conference*, 1, 2–7. https://doi.org/10.1109/fie.2002.1157954
- de Ries, K. E., Schaap, H., van Loon, A. M. M. J. A. P., Kral, M. M. H., & Meijer, P. C. (2022). A literature review of open-ended concept maps as a research instrument to study knowledge and learning. *In Quality and Quantity* (Vol. 56, Issue 1). Springer Netherlands. https://doi.org/10.1007/s11135-021-01113-x
- Dewey, John, and A. F. B. (1949). "Knowing and the Known." Boston Beacon Press.
- Gamble, Paul R., and J. B. (2001). "Knowledge management: A state of the art guide."
- Grundspenkis, J., & Strautmane, M. (2010). Usage of Graph Patterns for Knowledge Assessment Based on Concept Maps. Scientific Journal of Riga Technical University. Computer Sciences, 38(38), 60–71. https://doi.org/10.2478/v10143-009-0005-y
- Hamdiyati, Y., Sudargo, F., Redjeki, S., & Fitriani, A. (2018). Using concept maps to describe undergraduate students' mental model in microbiology course. *Journal of Physics: Conference Series*, 1013(1). https://doi.org/10.1088/1742-6596/1013/1/012014
- Henry, N. L. (1974). Knowledge Management: A New Concern for Public Administration. *Public Administration Review*, 34(3), 189. https://doi.org/10.2307/974902
- Jackson, K. M., & Trochim, W. M. K. (2002). Concept Mapping as an Alternative Approach for the Analysis of Open-Ended Survey Responses. *Organizational Research Methods*, 5(4), 307–336. https://doi.org/10.1177/109442802237114
- Kamble, S. K., & Tembe, B. L. (2013). The Effect of Use of Concept Maps on Problem Solving Performance and Attitude in Mechanical Engineering Course. *Procedia Social and Behavioral Sciences*, 83, 748–754. https://doi.org/10.1016/j.sbspro.2013.06.141
- Khajeloo, M., & Siegel, M. A. (2022). Concept map as a tool to assess and enhance students' system thinking skills. *Instructional Science*, 50(4), 571–597. https://doi.org/10.1007/s11251-022-09586-5
- Kinchin, I. M., Streatfield, D., & Hay, D. B. (2010). Using Concept Mapping to Enhance the Research Interview. *International Journal of Qualitative Methods*, 9(1), 52–68. https://doi.org/10.1177/160940691000900106
- Kumar, P., & Summers, J. D. (2024). Refining Engineering Identity Framework for Implementation In Engineering Education A Literature-Based Analysis. Volume 4: 21st International Conference on Design Education (DEC). https://doi.org/10.1115/DETC2024-143188
- Le Bras, P., Robb, D. A., Methven, T. S., Padilla, S., & Chantler, M. J. (2018). Improving user confidence in concept maps: Exploring data driven explanations. *Conference on Human Factors in Computing Systems Proceedings*, 2018-April, 1–13. https://doi.org/10.1145/3173574.3173978
- Lopez, E. J., Shavelson, R. J., Nandagopal, K., Szu, E., & Penn, J. (2014). Ethnically diverse students' knowledge structures in first-semester organic chemistry. *Journal of Research in Science Teaching*, 51(6), 741–758. https://doi.org/10.1002/tea.21160
- Mathieson, J. L., & Summers, J. D. (2010a). Complexity metrics for directional node-link system representations: theory and applications. *International Design Engineering Technical Conferences and Computers and Information in Engineering Conference*, 44137, 13–24.
- Mathieson, J. L., & Summers, J. D. (2010b). REPRESENTATIONS: THEORY AND APPLICATIONS. *DETC2010-28561*, 1–12.

- Mathieson, J., & Summers, J. D. (2017). A protocol for modeling and tracking engineering design process through structural complexity metrics applied against communication networks. *Concurrent Engineering Research and Applications*, 25(2), 108–122. https://doi.org/10.1177/1063293X16666936
- McClure, J. R., Sonak, B., & Suen, H. K. (1999). Concept map assessment of classroom learning: Reliability, validity, and logistical practicality. *Journal of Research in Science Teaching*, 36(4), 475–492. https://doi.org/10.1002/(SICI)1098-2736(199904)36:4<475::AID-TEA5>3.0.CO;2-O
- Moon, B., Johnston, C., & Moon, S. (2018). A case for the superiority of concept mapping-based assessments for assessing mental models. *International Conference on Concept Mapping*, 2008, 1–10.
- Novak, J. D. (2010). Learning Creating, and Using Knowledge (Second Edi, Vol. 0700). Routledge.
- Padilla, S., Methven, T. S., Robb, D. A., & Chantler, M. J. (2017). Understanding concept maps: A closer look at how people organise ideas. *Conference on Human Factors in Computing Systems Proceedings*, 2017-May, 815–827. https://doi.org/10.1145/3025453.3025977
- Patel, A., Summers, J. D., Kumar, P. P., & Edwards, S. L. (2024). Investigating the Use of Concept Maps and Graph-Based Analysis to Evaluate Learning. *ASEE Annual Conference and Exposition, Conference Proceedings*. https://doi.org/10.18260/1-2-47702
- Reichherzer, T., & Leake, D. (2006). Understanding the Role of Structure in Concept Maps. *Proceedings of the 28th Annual Conference of the Cognitive Science Society*, 2004–2009.
- Ruiz-Primo, M Araceli. (2004). Examining Concept Maps as an Assessment Tool. Concept Maps: Theory, Methodology, Technology. *Proc. of the First Int. Conference on Concept Mapping*, 1, 555–563.
- Ruiz-Primo, Maria Araceli, Shavelson, R. J., Li, M., & Schultz, S. E. (2001). On the validity of cognitive interpretations of scores from alternative concept-mapping techniques. *International Journal of Phytoremediation*, 21(1), 99–141. https://doi.org/10.1207/S15326977EA0702_2
- Rye, J. A., & Rubba, P. A. (2002). Scoring Concept Maps: An Expert Map-Based Scheme Weighted for Relationships. *School Science and Mathematics*, 102(1), 33–44. https://doi.org/10.1111/j.1949-8594.2002. tb18194.x
- Schau, C., Mattern, N., Zeilik, M., Teague, K. W., & Weber, R. J. (2001). Select-and-fill-in concept map scores as a measure of students' connected understanding of science. *Educational and Psychological Measurement*, 61(1), 136–158. https://doi.org/10.1177/00131640121971112
- Schroeder, N. L., Nesbit, J. C., Anguiano, C. J., & Adesope, O. O. (2018). Studying and Constructing Concept Maps: a Meta-Analysis. *Educational Psychology Review*, 30(2), 431–455. https://doi.org/10.1007/s10648-017-9403-9
- Tergan, S. O., Keller, T., & Burkhard, R. A. (2006). Integrating knowledge and information: Digital concept maps as a bridging technology. *Information Visualization*, 5(3), 167–174. https://doi.org/10.1057/palgrave.ivs. 9500132
- Torre, D. M., Daley, B., Stark-Schweitzer, T., Siddartha, S., Petkova, J., & Ziebert, M. (2007). A qualitative evaluation of medical student learning with concept maps. *Medical Teacher*, 29(9–10), 949–955. https://doi.org/10.1080/01421590701689506
- Trochim, W., & Kane, M. (2005). Concept mapping: An introduction to structured conceptualization in health care. *International Journal for Quality in Health Care*, 17(3), 187–191. https://doi.org/10.1093/intqhc/mzi038
- van Bon-Martens, M. J. H., van de Goor, L. A. M., Holsappel, J. C., Kuunders, T. J. M., Jacobs-van der Bruggen, M. A. M., te Brake, J. H. M., & Van Oers, J. A. M. (2014). Concept mapping as a promising method to bring practice into science. *Public Health*, 128(6), 504–514. https://doi.org/10.1016/j.puhe.2014.04.002
- Van Zele, E., Lenaerts, J., & Wieme, W. (2004). Improving the usefulness of concept maps as a research tool for science education. *International Journal of Science Education*, 26(9), 1043–1064. https://doi.org/10.1080/1468181032000158336
- Watson, M. K., Pelkey, J., Noyes, C. R., & Rodgers, M. O. (2016). Assessing Conceptual Knowledge Using Three Concept Map Scoring Methods. *Journal of Engineering Education*, 105(1), 118–146. https://doi.org/10.1002/jee.20111
- West, D. C., Park, J. K., Pomeroy, J. R., & Sandoval, J. (2002). Concept mapping assessment in medical education: A comparison of two scoring systems. *Medical Education*, 36(9), 820–826. https://doi.org/10.1046/j.1365-2923.2002.01292.x